# The Electronic Structure of Difluorophosphine, Difluorophosphine Oxide, and Difluorophosphine Borane

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The electronic structures of difluorophosphine  $(HPF_2)$ , difluorophosphine oxide  $(HPF_2O)$ , and difluorophosphine borane  $(HPF_2 \cdot BH_3)$  are examined by a non-empirical calculational procedure. The calculations reveal that the role of the d orbitals of phosphorus is important for HPF2O while their participation in the bonding of  $HPF_2$  and  $HPF_2 \cdot BH_3$  is still significant. The tilting of the BH<sub>3</sub> group within  $HPF_2 \cdot BH_3$  is found to stabilize the molecule by 8.41 kJ mol<sup>-1</sup>. The barrier to rotation about the P-Bbond for  $HPF_2 \cdot BH_3$  is calculated to be 23.09 kJ  $mot^{-1}$  in good agreement with experiment. In the eclipsed configuration of HPF<sub>2</sub>·BH<sub>3</sub>, the BH<sub>3</sub> moiety occupies a non-tilted position. The energies of formation of  $PH_3 \cdot BH_3$ ,  $HPF_2 \cdot BH_3$ , and  $PF_3 \cdot BH_3$ are calculated and the order of stability of these compounds is  $HPF_2 \cdot BH_3 > PF_3 \cdot BH_3 > PH_3 \cdot BH_3$  which agrees with experiment. Reasons are presented for the position of  $HPF_2 \cdot BH_3$  in this sequence.

# Introduction

Difluorophosphine borane (HPF<sub>2</sub>·BH<sub>3</sub>) has attracted a lot of attention ever since it was realised that it was quite stable at room temperature.<sup>1</sup> This is in complete contrast to the related compounds,  $F_3P \cdot BH_3$  and  $H_3P \cdot BH_3$ , which are highly dissociated at NTP. Recent structural investigations<sup>2</sup> revealed two additional intriguing features. First, the borane group is tilted away from the fluorine atoms so that the two PBH angles differ by approximately 10°. Second, the molecule adopts a staggered conformation with an estimated barrier to rotation of 15.06-18.83 kJ mol<sup>-1</sup> about the P-B bond. This rotational energy is high in comparison with the estimated barrier of 9.64 kJ mol<sup>-1</sup> and 0.37 kJ mol<sup>-1</sup> about the related B-N bond of BH<sub>3</sub>·NH<sub>3</sub><sup>3</sup> and BF<sub>3</sub>·NH<sub>3</sub><sup>3</sup> respectively. As the P-B and N-B bond differ mainly through the substitution of phosphorus 3p for nitrogen 2p orbitals and through the possible participation of 3d orbitals of phosphorus in the former, it is suggested that these are involved in  $\pi$ -bonding across the P-B bond and so are a hindrance to rotation. It is not permissible, however, to invoke the 3d orbitals of phosphorus as the reason for either the stability of  $HPF_2 \cdot BH_3$  or the tilt of the borane group, as  $PF_3 \cdot$ BH<sub>3</sub> would also be expected to have similar properties. The only obvious difference between these complexes is the presence of a P-H bond in HPF<sub>2</sub>·BH<sub>3</sub>. Hence interaction of this hydrogen with the borane group might be considered to bestow extra stability or the molecule. Therefore an ab initio investigation into the electronic structures of HPF<sub>2</sub>·BH<sub>3</sub> and its components HPF<sub>2</sub> and BH<sub>3</sub> was initiated to provide information about its unusual features. Calculations were also performed on difluorophosphine oxide (HPF<sub>2</sub>O), isoelectronic with HPF<sub>2</sub>·BH<sub>3</sub>, in order to compare the two different types of Lewis acid-Lewis base interactions and furthermore to examine the hydrogen-oxygen bonding for manifestations of a reactive hydrogen atom. Previous calculations on HPF<sub>2</sub>·BH<sub>3</sub> have been semi-empirical<sup>4</sup> and empirical<sup>2</sup> in nature.

The calculations were performed within the usual LCAO-MO-SCF framework in which the atomic orbitals are represented by linear combinations of gaussian functions. The 13s and 9p primitive gaussian functions of phosphorus are contracted to give 6s and 4p orbitals<sup>5</sup>, while for boron, fluorine and oxygen we combine the 9s and 5p gaussian functions to produce 4s and 2p atomic orbitals<sup>6</sup>. Four s functions contracted to two atomic orbitals simulate the 1s orbitals of hydrogen<sup>6</sup>. The 3d orbitals of phosphorus were represented by a linear combination of three gaussian functions chosen to reproduce a Slater type 3d orbital<sup>7</sup>. Preliminary calculations were performed to obtain an optimum Slater exponent for the 3d orbitals of phosphorus in HPF<sub>2</sub>. This exercise yielded 1.8 for the orbital exponent which was then used in the subsequent calculations. The structural information of the molecules was extracted from references 2, 8, 9 and 10.

## The Electronic Structure of HPF<sub>2</sub>

The gross atomic and overlap populations of HPF<sub>2</sub>, HPF<sub>2</sub>O, BH<sub>3</sub> and HPF<sub>2</sub> $\cdot$  BH<sub>3</sub> are presented in Table I.

TABLE I. The Atomic and Overlap Populations of HPF<sub>2</sub>, HPF<sub>2</sub>O, HPF<sub>2</sub>  $\cdot$  BH<sub>3</sub> and BH<sub>3</sub>.

Gross Atomic Populations						
	HPF <sub>2</sub>	HPF <sub>2</sub> O	$HPF_2 \cdot BH_3$	$BH_3$		
Р						
5	5.63	4.99	5.32	-		
p	8.18	7.89	8.19	-		
d	0.42	0.92	0.59			
total	14.23	13.79	14.10	-		
F						
\$	3.94	3.93	3.94	-		
p	5.50	5.46	5.46	-		
total	9.44	9.39	9.40	_		
В						
\$	_	_	3.08	3.12		
p		_	2,40	1.96		
total		_	5.48	5.08		
0	•					
\$	_	3.84	-	_		
p	_	4.72	_	-		
total	_	8.56	-	-		
H <sub>P</sub> s	0.90	0.84	0.83	-		
H <sub>BI</sub> s	_	-	0.91	0.97		
H <sub>B2</sub> s	-	_	0.94	0.97		
H <sub>B3</sub> s	-	-	0.94	0.97		
Overlap P	opulations					
H <b></b> −P	0.64	0.78	0.74	_		
F–P	0.42	0.58	0.50	_		
HpO	_	-0.04	-	-		
О–Р	_	1.30	_	-		
H <sub>P</sub> –B	_	-	-0.04	_		
P–B	_	_	0.36	_		
$B-H_{B1}$	_		0.84	0.82		
$B-H_{B2}$	-	-	0.82	0.82		

In  $HPF_2$  the phosphorus atom possesses a large positive charge due to donation of its valence electrons, mainly  $\pi$ -electrons, to the fluorines. The electrons of hydrogen are relatively unpolarised bestowing a small positive charge on the atom. A breakdown of the bond overlap populations reported in Table I reveals the nature of the bonding in the molecule. The P-H bond is largely composed of the phosphorus p  $\sigma$ -hydrogen s contribution (92%). The P<sub>d</sub>-H<sub>s</sub> component is small while the  $P_s-H_s$  content is antibonding. Similar features are present in the P-F bonds where the phosphorus s orbital is only slightly involved in the bonding. The p and d orbitals of phosphorus, however, form strong bonds with the fluorine porbitals. Close inspection of the wave function reveals that the  $\pi$ -bonding content is substantial. The highest filled orbital is largely localised on the s and p orbitals of phosphorus representing the classical picture of a lone pair of electrons in a  $sp^3$  hybrid. The main contribution to the first vacant orbital is a p orbital of the phosphorus perpendicular to the plane incorporating the P–H bond and bisecting the FPF angle.

#### The Electronic Structure of HPF<sub>2</sub>O

From the results of Table I we can observe the electronic distribution changes that have occurred as HPF<sub>2</sub> forms an oxide. The outcome is a large electron drift (0.56) towards oxygen from the HPF<sub>2</sub> group. The main source of the donated electrons is the phosphorus atom although the hydrogen and the two fluorines have also lost a small amount of electron density. It is interesting to note that this electron release has brought about an increase in the P-H and P-F bond populations due to increased participation in these bonds by the s and d orbitals of phosphorus. The P-O bond has a large overlap population emanating from interaction of the oxygen p orbitals with the phosphorus orbitals. The  $\pi$ -bond contribution, especially the  $P_d$ - $O_p$  component is a substantial part of the P-O bond. This component is also the cause of the increase in the electron  $\pi$  density of the phosphorus d orbital through back bonding with oxygen. The intramolecular O-H bond is weakly antibonding.

## The Electronic Structure of HPF<sub>2</sub> · BH<sub>3</sub>

The important feature of the electronic structure of  $HPF_2 \cdot BH_3$  is a donation of 0.27 electrons to the  $BH_3$ moiety. These released electrons stem largely from the phosphorus 3s orbital with a small amount from the hydrogen s and fluorine p orbitals. The borane group shows some interesting changes through coordination to  $HPF_2$ . The boron p orbitals have gained electrons while the s orbital population has diminished. The biggest orbital population change occurs in the boron p orbital which is vacant in planar BH<sub>3</sub> and is now occupied by 0.4 electrons. The hydrogen which is tilted towards the HPF<sub>2</sub> has gained electron density while the two hydrogens which are inclined away from the difluorophosphine have been deprived of electronic charge. The B-P bond consists of two large bonding components, namely  $P_s$ - $B_p$  and  $P_p$ - $B_p$ , coupled with an antibonding  $P_s$ - $B_s$  constituent. The  $\pi$ -bonding is not as important as it is in the P–O bond of HPF<sub>2</sub>O and accounts for  $\sim 20\%$  of the P-B overlap population. Coordination has caused a strengthening of the B-H bonds, the F-P bonds, and the H-P bonds.

From the orbital population data we can conclude that d orbital participation is important for HPF<sub>2</sub>O while its role in the bonding in HPF<sub>2</sub> and HPF<sub>2</sub> · BH<sub>3</sub> is still significant. This is also reflected in the changes in calculated total energies of the molecules when the d orbitals of phosphorus are omitted from the basis set. The resulting increase in energy of HPF<sub>2</sub>, HPF<sub>2</sub> · BH<sub>3</sub> and HPF<sub>2</sub>O is 288.2 kJ mol<sup>-1</sup>, 375.6 kJ mol<sup>-1</sup>, and 602.9 kJ mol<sup>-1</sup>, respectively.

#### The Electronic Structure of Non-tilted HPF<sub>2</sub>·BH<sub>3</sub>

So far, nothing has emerged from the above calculations which can explain the tilting of the borane moiety within  $HPF_2 \cdot BH_3$ . It was therefore necessary to obtain the electronic energies and orbital populations of  $HPF_2 \cdot BH_3$  in which  $BH_3$  has  $C_3$  symmetry with respect to the B–P axis. It was found (Table II) that the loss in stability due to adopting a non-tilting configuration is 8.41 kJ mol<sup>-1</sup>. The tilted configuration has a lower nuclear energy and although the nontilted structure has a more negative electronic energy, the nuclear energy change was the more dominant.

There is very little difference in the orbital populations of the two configurations. The main change is a small increase in the population of the hydrogens of the borane unit and a concomitant loss in electron density by the boron p orbitals. The non-tilted configuration displays an increase in the overlap populations of the P–B and P–F bonds in alliance with the more negative electronic energy. Perhaps the most interesting point to emerge from the overlap populaIn conclusion, we can state that the tilting of the borane group produces a decrease in the nuclear energy because the distortion is directed away from the fluorine atoms. At the same time, tilting causes an increase in the electronic energy and this is manifest in decreased overlap populations of the P–B and P–F bonds. However, there is an increase in bond populations involving the hydrogen atoms and the B–F bonds' population and this causes the electronic energy changes to be smaller than the nuclear energy changes.

#### Energy of Rotation about the P-B Bond

The eclipsed configuration of  $HPF_2 \cdot BH_3$  was calculated and the resulting energies and electronic popu-

TABLE II. The Electronic Ene	ergies and Populations of th	e Staggered and Eclipsed	I Configurations of HPF <sub>2</sub>	· BH <sub>1</sub> .
	<u> </u>			

	Staggered	Staggered		
	BH <sub>3</sub> tilted	BH <sub>3</sub> non-tilted	BH <sub>3</sub> tilted	BH <sub>3</sub> non-tilted
Electronic	·			
Energy	-751.78976	-752.36735	-752.72899	-752.47340
Nuclear				
Energy	185,16306	185.74384	186.11669	185.85551
Total				
Energy	-566.62670	-566.62351	-566.61230	-566.61789
Gross Atomic Pop	oulations			
Р	14.100	14.092	14.070	14.072
В	5.486	5.462	5.508	5.513
F	9.402	9.402	9.400	9.400
H <sub>B1</sub>	0.909	0.921	0.943	0.935
$H_{B2}, H_{B3}$	0.938	0.944	0.919	0.921
H <sub>P</sub>	0.837	0.832	0.842	0.840
Overlap Populatio	ons			
PF	0.504	0.520	0.508	0.508
P–B	0.358	0.450	0.490	0.446
PH∎	0.782	0.750	0.734	0.736
B-H <sub>P1</sub>	0.840	0.832	0.812	0.824
$B-H_{B2}$	0.816	0.808	0.810	0.804
B-H,	-0.034	-0.040	-0.052	-0.048
PH <sub>B1</sub>	-0.080	-0.126	-0.110	-0.108
$P-H_{B2}$	-0.086	-0.100	-0.198	-0.152
F-H <sub>B1</sub>	0.0002	0.0010	_	_
H <sub>B3</sub> -H <sub>P</sub>	-0.0006	0.0010	_	_
$H_{P}-H_{B1}$	_	_	0.0008	-0.0006
$H_{B2} - F_1$	_	_	0.0002	-0.0008
$H_{B3}-F_2$		_	0.0026	0.0022
B–F	-0.008	-0.010	-0.016	-0.014

lations are presented in Table II. The energy of rotation about the P–B bond is computed to be 37.78 kJ mol<sup>-1</sup> which is high in comparison with the experimental value. However it must be remembered that in this particular eclipsed form, the tilting of the BH<sub>3</sub> group might not attain the extra stability that is found in the staggered configuration. Therefore the energy and electronic structure of the eclipsed form of the non-tilted HPF<sub>2</sub>·BH<sub>3</sub> molecule were obtained. It was found (Table II) that the latter configuration is more stable than the eclipsed tilted conformation by 14.69 kJ mol<sup>-1</sup>. The barrier to rotation about the P–B bond is therefore 23.09 kJ mol<sup>-1</sup> in good agreement with the observed value.

The dominating energy term which determines the preferred eclipsed configuration is the nuclear energy contribution. The tilted-eclipsed configuration of  $HPF_2 \cdot BH_3$  has a more negative electronic energy but possesses larger antibonding interactions involving the hydrogen atoms and between the boron and fluorine atoms than is observed in the preferred non-tilted configuration.

It is now possible to compare the electronic changes which occur on rotation about the P-B bond. The phosphorus and fluorine atoms lose electron density while the boron atom becomes more negatively charged. However, it is the hydrogen atoms which display the most change. Both the hydrogen bonded to phosphorus gain electron density on rotation, while the remaining two hydrogen atoms release electrons during transformation to the eclipsed configuration. In general, rotation about the P-B bond causes the overlap population of the P-B and P-F bonds to increase while the remaining bonds suffer a loss. This decrease is particularly marked in the interactions between the borane hydrogens and phosphorus and for boron-fluorine bonds.

#### Energy of Formation of HPF<sub>2</sub> · BH<sub>3</sub>

In order to confirm the aforementioned sequence of stabilities of  $HPF_2 \cdot BH_3$ ,  $H_3P \cdot BH_3$ , and  $F_3P \cdot BH_3$ , the energies of formation ( $\Delta E_t$ ) were calculated for the reaction.

 $^{1}/_{2}$  B<sub>2</sub>H<sub>6</sub> + H<sub>x</sub>PF<sub>3-x</sub>  $\rightarrow$  H<sub>x</sub>PF<sub>3-x</sub>  $\cdot$  BH<sub>3</sub>

for x = 0, 1, and 3. The molecular dimensions of the molecules were taken from reference 2. It was found that  $\Delta E_f$  values for x = 0, 1, and 3 are +18.74 kJ mol<sup>-1</sup>, -15.19 kJ mol<sup>-1</sup> and +41.06 kJ mol<sup>-1</sup> respectively. These figures confirm that the order of stability is HPF<sub>2</sub>·BH<sub>3</sub> > F<sub>3</sub>P·BH<sub>3</sub> > H<sub>3</sub>P·BH<sub>3</sub>. It must be remembered that the above value is only one of many energy terms which constitute the free energy of reaction. It is thought that the stability sequence will not be altered by the inclusion of these terms but merely a change in absolute value of the energy terms will occur.

It has been suggested that the energy of reorganising the fluorophosphines into a configuration suitable for bonding to the borane may be a crucial factor in determining the relative stabilities of the borane complexes. Hence the energies of HPF<sub>2</sub> and PF<sub>3</sub> were recalculated using the coordinate system obtained for HPF<sub>2</sub>·BH<sub>3</sub> and PF<sub>3</sub>·BH<sub>3</sub>. This reorganisation involves contraction of the bond lengths and expansion of the inter-bond angles. The energy for such a transformation is 10.92 kJ mol<sup>-1</sup> and 7.38 kJ mol<sup>-1</sup> for PF<sub>3</sub> and HPF<sub>2</sub> respectively. Although the reorganisation energy is favourable for HPF<sub>2</sub> it is clearly not the dominating factor in determining the order of stability.

The energies of the highest filled and lowest empty orbitals of  $PF_3$ ,  $HPF_2$ , and  $PH_3$  along with the corresponding orbitals for their borane complexes are presented in Table III. It can be seen that  $HPF_2$  has the lowest-lying vacant orbital while only  $PH_3$  has a higher filled orbital than difluorophosphine. It is generally accepted that these orbitals play an important role in the formation of donor-acceptor complexes. Hence from a consideration of these orbital values,  $HPF_2$  would certainly appear to be a better Lewis base than either  $PH_3$  or  $PF_3$ . Moreover, when we examine the orbital values for the borane complexes we find that the stabilisation of the highest filled orbital due to complexing is greatest for  $HPF_2$ .

The electronic distribution of  $H_3P \cdot BH_3$  and  $F_3P \cdot$ BH3 were examined in order to rationalise the calculated energies of formation and the relevant information is listed in Table III. The electron density results reveal that there is an electron donation towards the borane unit of 0.28 e, 0.27 e, and 0.25 e for  $H_3P \cdot BH_3$ ,  $HPF_2 \cdot BH_3$ , and  $PF_3 \cdot BH_3$  respectively. For  $PH_3 \cdot$ BH<sub>3</sub> the source of this density is the phosphine hydrogen atoms while the s orbital population of phosphorus in PF<sub>3</sub> suffers the greatest loss upon complexing to BH<sub>3</sub>. The electron transfer process for HPF<sub>2</sub>·BH<sub>3</sub> is not too unexpectedly a hybrid of these two effects. The formation of the borane complexes increases the d orbital population of the phosphorus atom and this increase can be correlated with the decrease in the borane hydrogen population, the P-B bond population, and the number of fluorine atoms. Therefore it might be expected that  $F_3P \cdot BH_3$  would be the most stable complex. The reversal of order of stability for HPF<sub>2</sub>.  $BH_3$  and  $PF_3 \cdot BH_3$  must be due to the more antibonding long range forces present in the latter complex e.g. the B-F and P-H<sub>B</sub> bonds (Table III). Substitution of a fluorine atom in PF3 · BH3 by a hydrogen atom, with the subsequent tilting of the BH<sub>3</sub> group, causes a decrease in these interactions with a concomitant increase in the stability of HPF<sub>2</sub> · BH<sub>3</sub>.

In conclusion we can state that the order of stabilities,  $HPF_2 \cdot BH_3 > F_3P \cdot BH_3 > H_3P \cdot BH_3$  is due to several factors. The presence of fluorine atoms bonded

	PH <sub>3</sub>	HPF <sub>2</sub>	PF <sub>3</sub>	$PH_3 \cdot BH_3$	$HPF_2 \cdot BH_3$	$PF_3 \cdot BH_3$
Molecular Orbital						
Energies						
Highest						
filled (au)	-0.373	-0.419	-0.477	-0.400	-0.476	0.502
Lowest						
empty (au)	-0.168	0.137	0.141	0.118	0.130	0.145
Atomic Orbital Populations						
P s	5.78	5.63	5.58	5.63	5.32	5.16
p	9.38	8.18	7.65	9.36	8.19	7.73
d	0.17	0.42	0.52	0.25	0.59	0.72
to tal	15.33	14.23	13.75	15.24	14.10	13.61
F s	_	3.94	3.94	-	3.94	3.94
p	_	5.50	5.48	-	5.46	5.45
total	-	9.44	9.42	-	9.40	9.39
B s	_	-	_	3.02	3.08	3.11
p	-	-	-	2.45	2.40	2.39
to tal	<u> </u>	-	_	5.47	5.48	5.50
H <sub>B1</sub> s	-	_	-	0.94	0.91	0.92
$H_{B2}, B_{3}s$	-	_	_	0.94	0.94	0.92
H <sub>P</sub> s	0.89	0.90	-	0.82	0.83	-
Overlap Populatio	ns					
P-B	_	-	_	0.286	0.358	0.382
P–F	_	0.422	0.455	_	0.504	0.562
P-H <sub>p</sub>	0.659	0.647	-	0.702	0.782	-
B-H	_	_	_	0.808	0.840	0.824
B-H <sub>B2</sub>	_	_	_	0.808	0.816	0.824
P-Hp	_	-	_	-0.022	-0.034	_
B-H.	_	_	_	-0.009	-0.080	-0.105
$P - H_{B_2}$	-	-	_	-0.009	-0.086	-0.105
$H_{R2} - H_P$	_	_	_	-0.002	-0.0006	_
$H_{B1}-F_1$	-	_	-	<u> </u>	0.0002	-0.0002
B–F		_	-		-0.008	-0.010

TABLE III. The Electronic Distributions and Selected Orbital Energies of  $PH_3$ ,  $PF_3$ ,  $HPF_2$ ,  $PH_3 \cdot BH_3$ ,  $PF_3 \cdot BH_3$ , and  $HPF_2 \cdot BH_3$ .

to the phosphorus atom ensures that there is a strong P–B bond formed between the phosphine and borane groups. The greater stability of the difluoro derivative over the trifluorophosphine complex stems from smaller antibonding interactions present in  $HPF_2$ . BH<sub>3</sub>, a lower reorganisation energy of  $HPF_2$ , and more favourable orbital energies of  $HPF_2$ .

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